

EC317 – Labour Economics

Problem Set 10 Solutions

1. Consider the following equation for log-hourly wages

$$\ln(w_{it}) = \alpha + \beta d_{it}^{\text{union}} + x_i' \theta + \varepsilon_{it}, \quad (1)$$

where w_{it} is worker i 's hourly wage in wave $t \in \{1, 5\}$, d_{it}^{union} is a dummy indicating union membership in wave t , and x_i is a vector of time-invariant worker characteristics.

Obtain a cross-sectional estimate of the union wage differential β by OLS estimation of equation (1) for log-hourly wages in wave 1, controlling for the worker's age in wave 1 and its square, sex, and race. Weight your regression using the survey weights (variable **weight**) to account for the LFS stratified sampling design —type **help weight** and **help regress** in Stata to learn how to do this.

What is your estimate of the union wage differential?

Answer:

```
. regress lhw1 tu1 age1 age1sq sex white [pweight = weight], robust
(sum of wgt is 227,467,244.8949)
```

Linear regression	Number of obs	=	33,635
	F(5, 33629)	=	713.18
	Prob > F	=	0.0000
	R-squared	=	0.1473
	Root MSE	=	.51997

lhw1	Robust		t	P> t	[95% conf. interval]	
	Coefficient	std. err.				
tu1	.1113967	.0074065	15.04	0.000	.0968798	.1259137
age1	.0858845	.0020015	42.91	0.000	.0819614	.0898076
age1sq	-.0009723	.0000244	-39.85	0.000	-.0010201	-.0009245
sex	-.2183974	.0073544	-29.70	0.000	-.2328124	-.2039824
white	.0306437	.0195796	1.57	0.118	-.007733	.0690204
_cons	1.018546	.0438685	23.22	0.000	.9325616	1.104529

The point estimate $\hat{\beta}^{\text{cross}} = 0.111$ implies cross-sectional union wage differential of 11.1%.

2. Now, consider the *first-differenced* equation

$$\Delta \log(w_i) = \gamma + \beta \Delta d_i^{\text{union}} + \Delta \varepsilon_i \quad (2)$$

where $\Delta(\cdot)_i \equiv (\cdot)_{i5} - (\cdot)_{i1}$, and the intercept γ allows for a linear time trend in the underlying *levels* equation.

Estimate equation (2) by OLS. Again, use the survey weights.

What is your longitudinal estimate of the union wage differential β ? How does it differ from your cross-sectional estimate in question 1?

Answer:

```
. regress dlhw du [pweight = weight], robust
(sum of wgt is 227,467,244.8949)
```

Linear regression	Number of obs	=	33,635
	F(1, 33633)	=	10.90
	Prob > F	=	0.0010
	R-squared	=	0.0006
	Root MSE	=	.38945

dlhw	Robust		t	P> t	[95% conf. interval]	
	Coefficient	std. err.				
du	.0345348	.010462	3.30	0.001	.0140288	.0550407
_cons	.0383287	.0028503	13.45	0.000	.032742	.0439154

The point estimate $\hat{\beta}^{\text{longi}} = 0.035$ is around a third of the cross-sectional estimate $\hat{\beta}^{\text{cross}}$ from question 1, implying a longitudinal union wage differential of 3.5%

3. Notice that we can separate union membership changes across waves into two types of transition:

- (i) *union joiners*: $d_{i1}^{\text{union}} = 0$ and $d_{i5}^{\text{union}} = 1$
- (ii) *union leavers*: $d_{i1}^{\text{union}} = 1$ and $d_{i5}^{\text{union}} = 0$

Estimate a *first-differenced* equation like (2) but decomposing transitions $\Delta d_i^{\text{union}}$ into joiners and leavers. That is, run regression

$$\Delta \log(w_i) = \gamma + \beta_1 d_i^{\text{join}} + \beta_2 d_i^{\text{leave}} + \Delta \varepsilon_i, \quad (3)$$

where

$$d_i^{\text{join}} = \begin{cases} 1 & \text{if } d_{i1}^{\text{union}} = 0 \text{ and } d_{i5}^{\text{union}} = 1 \\ 0 & \text{otherwise} \end{cases} \quad \text{and} \quad d_i^{\text{leave}} = \begin{cases} 1 & \text{if } d_{i1}^{\text{union}} = 1 \text{ and } d_{i5}^{\text{union}} = 0 \\ 0 & \text{otherwise} \end{cases}.$$

Again, use the survey weights.

What are your estimates of the effects of joining and leaving unions? How do they compare to your results from question 2?

Answer:

```
. regress dlhw nu un [pweight = weight], robust
(sum of wgt is 227,467,244.8949)
```

Linear regression	Number of obs	=	33,635
	F(2, 33632)	=	5.54
	Prob > F	=	0.0039
	R-squared	=	0.0006
	Root MSE	=	.38946

dlhw	Robust					[95% conf. interval]
	Coefficient	std. err.	t	P> t		
nu	.0384568	.0144488	2.66	0.008	.0101367	.0667768
un	-.0299309	.0157944	-1.90	0.058	-.0608886	.0010267
_cons	.038013	.0029616	12.84	0.000	.0322082	.0438178

Point estimates $\hat{\beta}_1^{\text{longi}} = 0.038$ and $\hat{\beta}_2^{\text{longi}} = -0.03$ imply a wage increase of 3.8% when joining and a wage decrease of 3% when leaving a union, respectively. These estimates are close in magnitude to $\hat{\beta}^{\text{longi}}$ from question 2.

4. Using your results from question 3, perform a statistical test for symmetry of the effects of leaving/joining a union, i.e., for $H_0 : \beta_1 = -\beta_2$. Interpret your finding.

Answer:

```
. test nu = -un
( 1)  nu + un = 0
      F( 1, 33632) =    0.15
      Prob > F =    0.6959
```

We cannot reject the null hypothesis that $\beta_1 = -\beta_2$, as can be seen from the large p-value $p = 0.696$. This is a test of the implicit linearity assumption in equation (2) that the effects of changing membership status from 0 to 1 and from 1 to 0 are the same and equal to β . One way to see this is by noting that equation (2) can be rewritten as

$$\Delta \log(w_i) = \gamma + \beta d_i^{\text{join}} - \beta d_i^{\text{leave}} + \Delta \varepsilon_i \quad (2')$$

since

$$\Delta d_i^{\text{union}} = \begin{cases} 1 & \text{if } (d_{i1}^{\text{union}}, d_{i5}^{\text{union}}) = (0, 1) \\ 0 & \text{if } (d_{i1}^{\text{union}}, d_{i5}^{\text{union}}) \in \{(0, 0), (1, 1)\} \\ -1 & \text{if } (d_{i1}^{\text{union}}, d_{i5}^{\text{union}}) = (1, 0) \end{cases}$$

$$= d_i^{\text{join}} - d_i^{\text{leave}}$$

$$\implies \beta \Delta d_i^{\text{union}} = \beta d_i^{\text{join}} - \beta d_i^{\text{leave}}.$$

So, equations (2) and (3) are equivalent under H_0 .

5. Evaluate your results from questions 1–4 in light of the discussion about possible biases in cross-section and longitudinal estimates of the union wage differential. Briefly include a discussion of how misclassification of union status may affect this, in both the cross-section and longitudinal analysis.

Answer:

Cross-sectional estimates of the union wage differential most likely suffer from two main issues:

- (i) self-selection/sorting into union jobs
- (ii) misclassification of union status

Longitudinal estimates help us with (i) by removing any time-invariant individual effects. To fix ideas, suppose that $\varepsilon_{it} = \omega_i + \eta_{it}$ with η_{it} uncorrelated with union status and covariates x_i , but ω_i potentially correlated. First-differencing removes the ω_i unobserved individual effects so, to the extent that selection is on time-invariant unobservables, longitudinal estimates are free of selection bias.

However, under classical measurement error conditions, (ii) generates an attenuation bias in cross-sectional estimates that is exacerbated in longitudinal estimates. Therefore, it is not clear a priori whether the difference in estimates whereby $\hat{\beta}^{\text{longi}} < \hat{\beta}^{\text{cross}}$ stems from selection bias or attenuation bias due to measurement error. Also, notice that identification in the *first-differenced* specification comes from people moving in and out of union jobs, under the implicit assumption that these union status moves are random.